Effect of suppression of local distortion on the magnetic, electrical, and thermal transport properties of the Cr-substituted bilayer manganite LaSr$_2$Mn$_2$O$_7$

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We have investigated magnetic, electrical, and thermal transport properties (Seebeck effect and thermal conductivity) of LaSr$_2$Mn$_{2-x}$Cr$_x$O$_7$ polycrystalline samples ($y$=0.1, 0.2, 0.4, and 0.6). The Cr$^{3+}$ substitution for Mn$^{3+}$ sites causes a removal of $d_{z^2-r^2}$ orbital of $e_g$ electron, resulting in a volume shrinkage of the lattice. Magnetic measurements reveal the appearance of a glassy behavior for Cr-doped samples, accompanied by both a collapse of the A-type antiferromagnetic structure and the growth of ferromagnetic clusters. Cr-doping effect on electrical transport strongly enhances an insulating behavior over a wide range of temperatures, while it suppresses a local minimum of thermoelectric power at lower temperatures. For all polycrystalline samples with Cr substitution, the variable-range-hopping conduction model gives a reasonable fit to both resistivities and Seebeck coefficients. The phonon thermal conduction gradually rises with increasing Cr content, which is in contrast to a typical impurity effect on thermal conductivity. We attribute this to a suppression of local lattice distortion through the introduction of Jahn-Teller inactive ions of Cr$^{3+}$.

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I. INTRODUCTION

The discovery of colossal magnetoresistance (CMR) effect in doped manganites with perovskite structure has stimulated considerable interest for the understanding of their physical properties.1 Though the insulator-to-metal transition and its associated CMR are well explained on the basis of the double-exchange (DE) model, it is pointed out that the dynamic Jahn-Teller (JT) effect due to the strong electron-phonon interaction, plays a significant role in the appearance of CMR as well as the DE interaction.2,3 Furthermore, Dagotto et al. propose a phase separation model where the ferromagnetic (FM) metallic and antiferromagnetic (AFM) insulating clusters coexist and their model strongly supports recent experimental studies on the physics of manganites.4,5

In bilayer manganites La$_{2-x}$Sr$_{1+z}$Mn$_2$O$_7$, in which a MnO$_2$ bilayer is alternatively stacked with a (La,Sr)$_2$O$_2$ blocking layer along the $c$ axis, the physical properties strongly depend on hole doping level $x$.6 In particular, neutron diffraction study on half-doped LaSr$_2$Mn$_2$O$_7$ ($x=0.5$) has revealed the coexistence of the A-type antiferromagnetic phase and CE-type antiferromagnetic charge-ordered/orbital-ordered (CO/OO) phase.7 It is well known that the CE-type CO/OO state in cubic manganites is unstable against Cr substitution for Mn site, and light Cr doping up to a few percent yields a drastic collapse of the CO/OO phase, resulting in a FM metallic phase even in the absence of any applied magnetic field.8-9 While several reports on the effect of Cr substitution on the physical properties of the cubic manganites have appeared, very few reports have appeared on such studies in the case of bilayer manganites.10,11 Here, we give some comments on pressure effect on a two-dimensional network of MnO$_6$ octahedra in bilayer manganites La$_{1.2}$Sr$_{1.8}$Mn$_2$O$_7$. Argyriou et al.12 reported that the Mn—O(3)—Mn bond angle is almost unchanged by application of pressure, indicating no tilting of the MnO$_6$ octahedra in the $ab$ plane. Thus, it is possible to examine the internal and external pressure effect in bilayer manganites, varying the bond length of the MnO$_6$ octahedra but keeping the bond angle almost $180^\circ$. In this paper, we report magnetic, electrical, and thermal transport properties of single-phase LaSr$_2$Mn$_{2-y}$Cr$_y$O$_7$ polycrystalline samples ($y=0.1, 0.2, 0.4, 0.6$). The Cr substitution for Mn sites causes a monotonic shrink of the $a(b)$ axis in contrast with a gradual elongation of the $c$ axis, accompanied by $d_{x^2-y^2}$ orbital deficiencies of $e_g$ electron, as listed in Table I. The 3$d$ electronic state of Cr$^{3+}$ ion is taken as $t^3_2e_g^0$ (spin quantum number $S=3/2$), resulting in undistorted CrO$_6$ octahedron sites free from a local Jahn-Teller effect. This finding is quite reasonable with a volume shrinkage of MnO$_6$ octahedra in bilayer manganites La$_{1.2}$Sr$_{1.8}$Mn$_2$O$_7$.

### Table I. The lattice parameters $a$ and $c$. A-type AFM transition temperature $T_N$, spin-glass-like transition temperature $T_{SG}$.

<table>
<thead>
<tr>
<th>Sample $y$</th>
<th>$a$ (Å)</th>
<th>$c$ (Å)</th>
<th>$T_N$ (K)</th>
<th>$T_{SG}$ (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>3.8790</td>
<td>19.996</td>
<td>210</td>
<td></td>
</tr>
<tr>
<td>0.1</td>
<td>3.8716</td>
<td>20.020</td>
<td>175</td>
<td></td>
</tr>
<tr>
<td>0.2</td>
<td>3.8660</td>
<td>20.030</td>
<td>130</td>
<td></td>
</tr>
<tr>
<td>0.4</td>
<td>3.8571</td>
<td>20.062</td>
<td>38</td>
<td></td>
</tr>
<tr>
<td>0.6</td>
<td>3.8562</td>
<td>20.094</td>
<td>34.5</td>
<td></td>
</tr>
</tbody>
</table>

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age observed due to Cr doping because a removal of \(d_{z^2-r^2}\) orbital from Mn\(^{3+}\) sites easily causes a suppression of local lattice distortion, as discussed later. In the parent material LaSr\(_2\)Mn\(_2\)O\(_7\), a majority phase of the A-type AFM state coexists with a minority phase of CE-type AFM charge-ordered/orbital-ordered state.\(^7\) We focus our attention on the Cr-doping effect on the A-type AFM majority phase because it is expected that the CO/OO minority phase is strongly suppressed by Cr doping.

**II. EXPERIMENT**

Polycrystalline samples of LaSr\(_2\)Mn\(_{2-x}\)Cr\(_x\)O\(_7\) (\(y=0.1, 0.2, 0.4, \) and 0.6) were synthesized by solid-state reaction of La\(_2\)O\(_3\), SrCO\(_3\), MnO\(_2\), and Cr\(_2\)O\(_3\) powders with high purity. The oxygen concentration of typical samples with \(y=0.2\) and 0.6 was determined using the infrared absorption method because the existence of the Cr ions may affect the valence estimation of the Mn ion made by the chemical analysis. The composition of cations was examined by inductively coupled plasma analysis. For the \(y=0.2\) and 0.6 samples, we got La\(_{1.01}\)Sr\(_{1.95}\)Mn\(_{1.41}\)Cr\(_{0.59}\)O\(_{7.05}\) at \(y=0.6\). Thus, we conclude that our samples prepared by the solid-state reaction technique are close to nominal compositions. Let us consider the difference in oxygen concentration (hole concentration). The values of \(7-\delta=6.99\) at \(y=0.2\) and 7–\(\delta=7.05\) at \(y=0.6\) give hole contents of \(x=0.5\) and \(x=0.55\), respectively. Recent neutron powder diffraction studies on La\(_{2.24}\)Sr\(_{1.76}\)Mn\(_2\)O\(_7\) revealed the magnetic and crystallographic phase diagram in the region \(x>0.5,\)\(^13\) In particular, when \(0.42<x<0.66\), the A-type AFM state with antiferromagnetic coupling appears along the \(c\) axis between FM single layers within one bilayer. We believe that the excess oxygen content \((x=0.55)\) has little effect on the magnetic property because the AFM magnetic transition temperature is stable over the range of hole concentration up to \(x=0.6\).

The x-ray powder diffraction patterns were recorded for all samples on a RIGAKU diffractometer with Cu \(K\alpha\) radiation, as depicted in Fig. 1. The x-ray data are indexed in terms of (La,Sr)\(_2\)Mn\(_2\)O\(_7\) 327 phase except for a small amount of impurity phase, indicating a single phase of bilayered structure. The lattice parameters calculated using the least-squares fits are listed in Table I as a function of Cr content.

Magnetic measurements as a function of temperature were carried out using a superconducting quantum interference device magnetometer in both zero-field-cooled (ZFC) and field-cooled (FC) scans. The magnetic relaxation was measured as follows. First, the sample was cooled down to the respective temperatures in a zero field and then the applied field was held for 5 min. Finally, just after the field was switched off, remanent magnetization data were recorded as a function of time. Electrical resistivity was measured by a conventional four-probe technique. Magnetoresistance measurements were performed at National Institute for Materials Science. Here, an electric current supplied was parallel to the direction of the external field. The thermal conductivity was measured using a conventional heat-flow method. The thermoelectric power \(S=(dV/dT)\) was determined both from a temperature gradient and thermoelectric voltage, \(dV\) and \(dT\), which are generated from a thermal current in the longitudinal direction of samples.

**III. RESULTS AND DISCUSSION**

**A. Magnetic property**

First, we show in Fig. 2 the ZFC and FC temperature dependences of the magnetization in polycrystalline LaSr\(_2\)Mn\(_{2-x}\)Cr\(_x\)O\(_7\) \((y=0.1, 0.2, 0.4, \) and 0.6) measured at 10 mT. For comparison, the \(ab\)-plane magnetization data of parent crystal LaSr\(_2\)Mn\(_2\)O\(_7\) are presented in the inset of Fig. 2.\(^14\) Upon cooling the Cr-free sample, a broad maximum in \(M_{ab}\) is observed near about 210 K, associated with the A-type AFM transition.\(^15,16\) Cr doping strongly suppresses Néel temperature \(T_N\), from 210 K at \(y=0.1,\) through 175 K at \(y=0.2,\) down to 130 K at \(y=0.6,\) and such a magnetic anomaly finally disappears for the \(y=0.4\) and 0.6 samples. The \(T_N\) is determined from a local maximum at higher temperatures in ZFC data. In the A-type AFM structure, FM spins lying in \(ab\) plane of the respective MnO\(_2\) single layer are antiferromagnetically coupled along the \(c\) axis within a MnO\(_2\) double layer. We expect that a partial substitution of Cr\(^{3+}\) for Mn\(^{3+}\) sites causes \(d_{z^2-r^2}\) orbital deficiencies of \(e_g\) electron and weakens an AFM coupling working between respective single layers, resulting in an observed drop of \(T_N\). Instead, a low-\(T\) peak in ZFC scan rapidly grows with Cr doping, ac-

![FIG. 1. (Color online) (a) The x-ray powder diffraction pattern on the \(y=0.4\) sample. Dots and a solid line are the observed and calculated intensities, respectively. The x-ray data are indexed in terms of (La,Sr)\(_2\)Mn\(_2\)O\(_7\) 327 phase except for a small amount of impurity phase. (b) The lattice parameters calculated using the least-squares fits as a function of Cr content, as listed in Table I.](image-url)
accompanied by a hysteresis region surrounded between ZFC and FC curves. At further low temperatures, the ZFC magnetization of \( y = 0.2 - 0.6 \) shows a steep decrease, indicating the freezing of magnetic moments.\(^{17,18} \) These findings are reminiscent of magnetic behaviors of a standard spin-glass system due to a magnetic frustration between ferromagnetic and antiferromagnetic interactions.\(^{19} \) A characteristic temperature at which the prominent peak in ZFC scan is located at low \( T \) is defined as \( T_{SG} \) for the \( y = 0.4 \) and 0.6 samples at 10 mT. In addition, the temperature variation of the magnetization in polycrystalline \( \text{LaSr}_2\text{Mn}_{2-y}\text{Cr}_y\text{O}_7 \) both in 0.1 and 1 T are shown in Fig. 3. At 0.1 T, a history effect between ZFC and FC scans remains visible at lower \( T \). However, at a relatively high field of 1 T, the irreversibility in magnetization curves is strongly suppressed and a ferromagnetic-like behavior appears at low temperatures. These tendencies depending on the applied fields are never observed in a conventional spin-glass system.

Next, we examine the field dependence of low-\( T \) magnetization in \( \text{LaSr}_2\text{Mn}_{2-y}\text{Cr}_y\text{O}_7 \) \( y = 0.1, 0.2, 0.4, \) and 0.6) [Fig. 4(a)]. The \( ab \)-plane magnetization of the Cr-free crystal shows a linear dependence on the field, in association with an AFM spin canting induced by the external field.\(^{16} \) On the other hand, in Cr-doped samples, \( M-H \) curves rise rapidly at low fields and then tend to saturate up to a maximum field of 5 T, indicating the development of ferromagnetic states. Upon increasing Cr doping, the initial \( M \) shows a steeper rise. We show in Fig. 4(b) the saturated magnetization at 5 T plotted as a function of Cr content. We notice that the saturated magnetic moment \( M_{sat} \) is almost independent of Cr impurities, in strong contrast to the Cr-substitution effect on low-field magnetization in the inset of Fig. 4(b). It is true that Cr impurity induces ferromagnetic moment from the inset of Fig. 4(b), but the volume fraction of FM phase at 5 T is almost insensitive of Cr content. The value of \( M_{sat} \) at 5 T is converged within 30% to 35% of full ferromagnetic moment. \( M_{full} = 3.4 \) \( \mu_B \) at \( y = 0.2 \) and \( M_{full} = 3.2 \) \( \mu_B \) at \( y = 0.6 \).
substitution effect between low- and high-field magnetic properties. A partial substitution of Cr$^{3+}$ ion for Mn$^{3+}$ suppresses not only AFM coupling between single MnO$_2$ layers but also destroys FM double-exchange interaction between Mn$^{3+}$ and Mn$^{4+}$ ions within the MnO$_2$ layer. It is expected that the addition of Cr$^{3+}$ ions causes a suppression of the FM regions mediated by DE interaction through removing Mn$^{3+}$ ions. On the other hand, the low-field data support the occurrence of the ferromagnetic moment induced by Cr substitution. Following the Kanamori-Goodenough rules, the super-exchange (SE) interaction between Cr$^{3+}$ ($t_{2g}^5e_g^0$) and Mn$^{3+}$ ($t_{2g}^5e_g^0$) ions is ferromagnetic, while the SE interaction between Cr$^{3+}$ and Mn$^{4+}$ ($t_{2g}^5e_g^0$) becomes antiferromagnetic.20 The annihilation of the Mn$^{3+}$-Mn$^{3+}$ FM pairs is compensated by the creation of the Cr$^{3+}$-Mn$^{3+}$ FM pairs accompanied by the Cr$^{3+}$-Mn$^{4+}$ AFM pairs. In other words, the DE-driven FM regions are partially replaced by the SE-driven FM regions with increasing the Cr ions, keeping the total FM fraction. The FM double-exchange interaction between Mn$^{3+}$ and Cr$^{3+}$ is not possible in our samples because the occurrence of FM moment by Cr doping accompanies no metallic property, as discussed later in the Cr-doping effect on resistivity. At high fields, the phase separation between the field-induced FM phase and AFM second phase is probably realized at the level of clusters on the basis of the competition between FM and AFM interaction.

Next, we carried out the magnetic relaxation of the y=0.4 sample in order to examine the glassy state below $T_{SG}$. In Fig. 5, we show the remanent magnetization data of the y=0.4 sample as a function of time, just after holding an applied field $H_a$ for 5 min and then switching it off. At 10 mT, the magnetization relaxes more quickly at lower $T$, in contrast with the $M(t)$ data at 100 mT. However, at 1 T no slow relaxation in $M$ is observed, which is consistent with no historical effect in ZFC and FC scans. The slow decay of remanent magnetization curves indicates that a difference in free energy between the present excited and ground states is quite small in comparison with thermal energy, and the system remains stable in various excited states.21–23 Thus, a relatively fast relaxation of remanent $M$ at 10 K in the 10 mT scan leads to a larger difference of energy barrier between the ground and excited states than in the case of 100 mT at the same temperature. The metastable state excited by the lower field is probably related to the degree of a magnetic frustration between AFM and FM clusters and/or the spatial distribution of frustrated clusters. Furthermore, the coexistence of frustrated clusters and ferromagnetic clusters plays a crucial role in the magnetic relaxation in 100 mT. FM spins and/or FM domain walls are pinned on the lattice defect sites like an oxygen vacancy, giving a longer relaxation time.

B. Electrical transport property

Figure 6 displays the temperature dependence of the electrical resistivity in polycrystalline LaSr$_2$Mn$_{2-y}$Cr$_y$O$_7$ (y=0.1, 0.2, 0.4, and 0.6). For comparison, the resistivity data of parent crystal LaSr$_2$Mn$_2$O$_7$ are also presented.22 For $y=0.1$, 0.2, 0.4, and 0.6, Cr doping strongly enhances an insulating behavior over a wide range of temperatures because conduction paths are partially destroyed by $d_{x^2-y^2}$ orbital deficiencies of the $e_g$ electron. Our data exclude in this system a possibility of the global double-exchange interaction between Mn$^{3+}$ and Cr$^{3+}$ ions, giving a metallic property.24 In particular, for the $y=0$–0.2 sample, the rapid rise in $\rho(T)$ below 50 K is close to a carrier localization effect due to a suppression of carrier hopping between single layers because at lower-$T$, orbital fluctuation of $d_{x^2-y^2}$ is gradually suppressed and motion of carriers is confined within the respective single layer.16

We try to analyze the $\rho(T)$ data of Cr-doped samples using the small-polaron hopping model and Mott’s variable-
range-hopping (VRH) model,\textsuperscript{25} to examine the conduction mechanism of bilayered manganites.\textsuperscript{26} According to Mott’s VRH model, the temperature dependence of resistivities is represented by $\rho(T) = \rho_0 T^{1/4} \exp([T_0/T]^d)$, where $\rho_0$ is a constant and $p=1/(d+1)$, with $d$ being the dimensionality of the system. Mott’s activation energy $T_0$ is proportional to $1/[N(E)\xi^d]$, where $N(E)$ is the density of states at the Fermi level and $\xi$ is the localization length. On the other hand, the adiabatic small-polaron model is described by $\rho(T) = \rho_0 T \exp(E_p/kT)$, where $\rho_0$ is a constant and $E_p$ represents the activation energy of a small polaron. For all samples with Cr substitution, it is found that the VRH model gives a more reasonable fit to the experimental data over a wide range of temperatures, in comparison with the small-polaron model. In Fig. 7(a), we present our results as a semilog plot of $\rho$ versus $T^{-p}$ with $p=1/3$ for two-dimensional (2D) VRH, while the inset of Fig. 7(a) shows a semilog plot of $\rho$ versus $T^{-p}$ with $p=1/4$ for three-dimensional (3D) VRH. Although it is hard to distinguish a $T^{-1/3}$ or $T^{-1/4}$ dependence of $\ln \rho$, we obtain a much better fit to Mott’s VRH than to a VRH model with $p=1/2$ in the presence of a Coulomb gap.\textsuperscript{26,27} The fitting parameters, $\rho_0$ and $T_0$, for polycrystalline samples of LaSr$_2$Mn$_{2-x}$Cr$_x$O$_7$ ($y=0.1, 0.2, 0.4,$ and 0.6) are listed in Table II. With increasing Cr content, the value of $T_0$ shows a monotonic increase for both 2D and 3D cases, indicating the decrease of the localization length $\xi$. The localization effect, enhanced due to Cr substitution, is probably associated with orbital disorders in Mn-O-Mn networks introduced by the removal of the $t_2g$ electron.\textsuperscript{28,29}

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|}
\hline
Sample & $y$ & VRH & 2D VRH & 3D VRH \\
\hline
& & & $\rho_0$ (\Omega cm) & $T_0$ (K) & $\rho_0$ (\Omega cm) & $T_0$ (K) \\
\hline
& & & & & \\
0.1 & $T>187$ & $2.1 \times 10^{-6}$ & $1.0 \times 10^{-6}$ & $8.7 \times 10^{-9}$ & $5.4 \times 10^{-9}$ \\
& $T>161$ & $3.0 \times 10^{-6}$ & $1.2 \times 10^{-6}$ & $8.1 \times 10^{-9}$ & $7.0 \times 10^{-9}$ \\
& $T>155$ & $2.0 \times 10^{-6}$ & $1.5 \times 10^{-6}$ & $3.7 \times 10^{-9}$ & $8.9 \times 10^{-9}$ \\
& $T>113$ & $2.6 \times 10^{-6}$ & $1.8 \times 10^{-6}$ & $2.7 \times 10^{-9}$ & $1.2 \times 10^{-9}$ \\
\hline
\end{tabular}
\caption{The fitting parameters $\rho_0$ and $T_0$ for polycrystalline samples of LaSr$_2$Mn$_{2-x}$Cr$_x$O$_7$ ($y=0.1, 0.2, 0.4,$ and 0.6).}
\end{table}

We give some comments on the doping effect of other trivalent metallic ions (Co$^{3+}$ and Al$^{3+}$) on the Mn sites of La$_3$Sr$_2$Mn$_3$O$_{7-\delta}$.\textsuperscript{28,29} The 3$d$ electronic configuration of Co$^{3+}$ ion follows as $t_{2g}^2e_g^0$ ($S=0$, low-spin state), $t_{2g}^2e_g^1$ ($S=1$, intermediate-spin state), and $t_{2g}^2e_g^2$ ($S=2$, high-spin state). The Al$^{3+}$ ion is a nonmagnetic ion without $d$ electrons. With increasing Co$^{3+}$ (or Al$^{3+}$) doping level, the A-type AFM temperature shifts to low temperatures and the magnitude of magnetization decreases over a wide range of temperatures. The decrease of $M$ implies a reduction of the net magnetic moments, which is consistent with low-spin state ($S=0$) of Co$^{3+}$ or nonmagnetic ion of Al$^{3+}$. The latter tendency is in strong contrast with the magnetic effect of Cr$^{3+}$ $(t_{2g}^2e_g^0, S=3/2)$ doping on La$_3$Sr$_2$Mn$_3$O$_{7-\delta}$, although a suppression of A-type AFM temperature is commonly observed for Cr, Co, and Al doping. On the other hand, the doping effects on electrical transport for Cr, Co, and Al ions exhibit such common features as the enhanced insulating state due to orbital deficiencies following the VRH model. In particular, the Al substitution without $d$ electrons for the Mn site produces a more rapid increase in resistivities.

Magnetoresistance effect of the $y=0.2$ sample as a function of temperature is depicted in Fig. 7(b), where the negative MR is defined as $-100(\rho(T) - \rho(0 \, \text{K})/\rho(0 \, \text{K})$. The value of giant MR increases from 25% at 150 K up to 80% at 4.2 K with decreasing $T$. The existence of the field-induced FM clusters is probably related to the enhanced MR at low temperatures, as we see from $M$-$T$ data in Fig. 3(b). In the inset of Fig. 7(b), the MR of $y=0.1$ and 0.2 samples is plotted as a function of field up to 8 T. Cr doping also increases a low-$T$ MR from 45% at $y=0.2$ up to 80% at $y=0.6$ under a field of 8 T at 40 K. The Cr-doping-induced orbital disorders assist charge transfer along the $c$ axis across the respective single layers of MnO$_2$, giving the enhanced MR effect.

C. Thermal transport properties (Seebeck coefficient and thermal conductivity)

Next, the temperature variation of Seebeck coefficient $S$ for the $y=0.1–0.6$ samples is displayed in Fig. 8(a). For comparison, the $S(T)$ data of single crystalline LaSr$_2$Mn$_2$O$_4$ are cited.\textsuperscript{14} For $y=0–0.2$, with decreasing $T$, the value of $S(T)$ shows a local maximum near the A-type AFM transition temperature $T_N$, and then a shallow minimum at lower $T$ is observed.\textsuperscript{30} At lower $T$, Cr doping gradually suppresses a local minimum of $S(T)$ from a negative value at $y=0$ down...
to a small one at $y=0.2$, and finally at $y=0.4$ the local minimum in $S(T)$ disappears, giving a monotonic decrease over the observed temperature range. Now, let us try to analyze the $S(T)$ data of Cr-doped samples using the extended Mott’s VRH model to seebeck coefficients.\textsuperscript{25,31} For the 2D VRH case, the corresponding form is described by $S(T) \propto T^{\nu}$ with $\nu=1/3$ ($\nu=1/2$ for the 3D VRH case). In Fig. 8(b), we present our results as a linear plot of $S(T)$ versus $T^{1/3}$ for 2D VRH (in the inset, $S(T)$ versus $T^{3/2}$ for 3D VRH). In a similar way, we obtain a much better fit of $S(T)$ data to the VRH law than to the thermally activated $T$ dependence. Here, the Seebeck coefficient for a thermally activated case is expressed as $S(T) = kT/E_k + S_a$, where $E_k$ is a thermal activation energy and $S_a$ denotes Seebeck coefficient in the high-temperature limit. In addition, the obvious differences among the $T$, $T^{1/2}$, and $T^{3/3}$ dependences we do not notice within our fitting procedures. In the random hopping system, the $T$-linear dependence of $S(T)$ is presented theoretically by Culter and Mott.\textsuperscript{32} The $T$-linear dependence of $S(T)$ in the insulating state is probably related to a random distribution of localized electronic states around the Fermi level, as reported in Seebeck coefficient of $Li_{1+y}Ti_{2−y}O_4$ oxides.\textsuperscript{33}

In a doped bilayer manganite with hole content $x=0.4$, the high-temperature behavior of $S(T)$ is well explained on the basis of a model of Zener polarons, where a Zener polaron formed in the high-$T$ region occupy two manganese sites.\textsuperscript{34} It is true that this model qualitatively reproduces a negative sign in high-$T$ behavior of single crystalline $La_1Sr_2Mn_2O_7$. However, for all polycrystalline samples with Cr substitution, it seems that the VRH conduction gives a reasonable fit to both resistivities and Seebeck coefficients.

Finally, let us show in Fig. 9 the thermal conductivity of Cr-doped $LaSr_2Mn_{2−y}Cr_yO_7$ ($y=0.1, 0.2$, and $0.4$) as a function of temperature. For comparison, the $\kappa$ data of polycrystalline $Sr_3Mn_2O_7$ ($x=1$) are presented. For comparison, the $\kappa$ data of polycrystalline $Sr_3Mn_2O_7$ ($x=1$) are presented.\textsuperscript{35} First of all, thermal carries are phonons since the electron component is estimated to be negligible from the resistivity data using the Weidemann-Franz law. The phonon thermal conduction gradually increases with Cr doping, which seems to be an unusual behavior because the introduction of Cr-impurity ions would disturb phonon conduction. However, this anomalous finding is reasonably resolved through clarifying a close relationship between phonon conduction and local lattice distortion of MnO$_6$ due to the Jahn-Teller effect. In our previous work on thermal conductivity in bilayered manganite single crystals, it was made clear that the phonon conduction in the insulating state is scattered by local lattice distortions due to a screening effect of itinerant carriers.\textsuperscript{35} It is true that this model qualitatively reproduces a negative sign in high-$T$ behavior of single crystalline $La_1Sr_2Mn_2O_7$. However, for all polycrystalline samples with Cr substitution, it seems that the VRH conduction gives a reasonable fit to both resistivities and Seebeck coefficients.
duction. Surely, the $\kappa(T)$ of polycrystalline Sr$_2$Mn$_2$O$_7$ ($x$ =1) shows a typical phonon conduction, whose behavior is free from JT distortion of Mn$^{3+}$O$_6$. In addition, the Cr-doping dependence of $a$- and $c$-axis lattice parameters in Table I reveals the volume shrinkage of the unit cell with increasing Cr content, as shown in Fig. 8(b). We note that the lattice constant of $y$=0.6 is influenced by a small amount of the impurity phase. This volume effect is associated with a number of deficiencies of $d_{x^2-y^2}$ orbitals of the $e_g$ electron, which is quite consistent with the preceding discussion on the close relationship between the lattice distortion and phonon conduction.

**IV. SUMMARY**

We have carried out magnetic, electrical, Seebeck effect, and thermal conductivity measurements of LaSr$_2$Mn$_{2-x}$Cr$_x$O$_7$, polycrystalline samples ($y$=0.1, 0.2, 0.4, and 0.6). The Cr$^{3+}$ substitution for Mn$^{3+}$ sites produces a monotonic shrink of the $a(b)$ axis in contrast with a gradual elongation of the $c$ axis in association with a removal of the $d_{x^2-y^2}$ orbital of the $e_g$ electron. For Cr-doped samples, a glassy behavior appears, accompanied by both a collapse of the A-type antiferromagnetic property and the development of ferromagnetic clusters. At high fields, the irreversibility in magnetization curves disappears and the saturated magnetic moment induced by the applied field reaches 30% to 35% of full ferromagnetic moment at 5 T for all Cr-doped samples. This finding strongly suggests the presence of a phase separation between FM and second phases at the level of clusters, which originate from the frustration between FM and AFM interactions. The electrical transport for Cr-doped samples strongly enhances an insulating property over the wide range of temperatures because conduction paths are partially destroyed by $d_{x^2-y^2}$ orbital deficiencies of the $e_g$ electron. At lower $T$, Cr doping gradually suppresses a local minimum of $S(T)$ from a relatively large value at $y$=0 down to a positively small one at $y$=0.4, in striking contrast to the more enhanced low-$T$ resistivity data. For all polycrystalline samples with Cr substitution, it seems that the VRH conduction gives a reasonable fit to both resistivities and Seebeck coefficients. The phonon thermal conduction gradually increases with increasing Cr content, which is in contrast to a typical impurity effect on thermal conductivity. We propose that the increase in the phonon thermal conduction results from a suppression of local lattice distortion through the introduction of a Jahn-Teller inactive ion of Cr$^{3+}$.

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